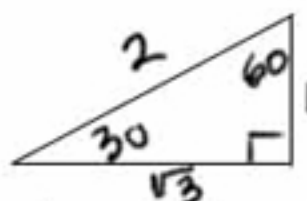
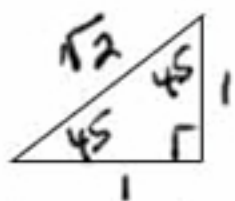


# 13-4 Graphs of the Sine and Cosine Functions Page 624

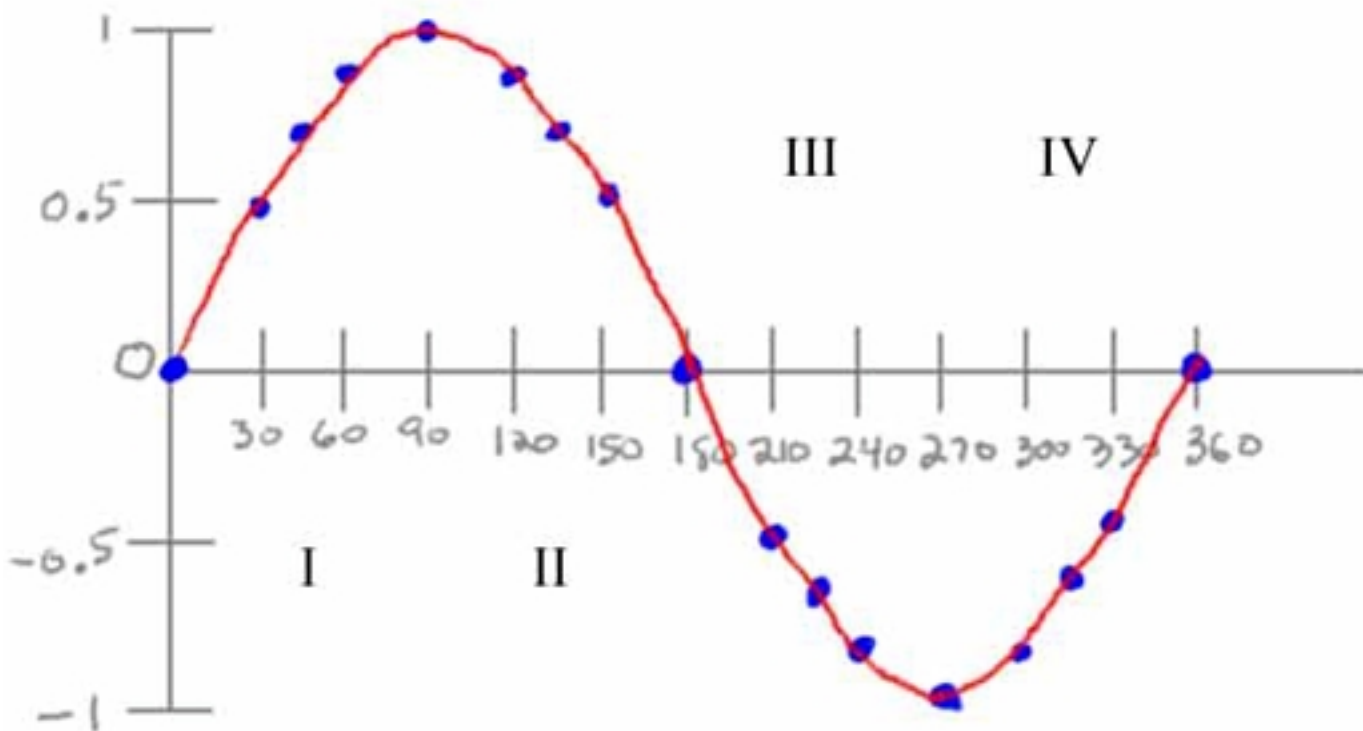
To graph  $y = \sin \theta$  we will have to remember several values of the sine function.



$$\sqrt{2} \approx 1.414$$

$$\sqrt{3} \approx 1.732$$

Degrees	0	30	45	60	90	120	135	150	180	210	225	240	270	300	315	330	360
Radians	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{3\pi}{4}$	$\frac{5\pi}{6}$	$\pi$	$\frac{7\pi}{6}$	$\frac{5\pi}{4}$	$\frac{4\pi}{3}$	$\frac{3\pi}{2}$	$\frac{5\pi}{3}$	$\frac{7\pi}{4}$	$\frac{11\pi}{6}$	$2\pi$
Sin $\theta$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{3}}{2}$	-1	$-\frac{\sqrt{3}}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{1}{2}$	0



For Homework you will follow the above example and graph the Cosine function.

Sine and Cosine are called **Periodic Functions** because their basic shape repeats every  $360^\circ$  or  $2\pi$  radians. The period for these two functions is therefore,  $360^\circ$  or  $2\pi$  radians.

Think of the Sine curve as a horizontal "**S**" shape and Cosine as a "**U**" shape.

Let's look at general Sine and Cosine functions and their graphs

$$y = A \sin B\theta$$

$$y = A \cos B\theta$$

**A** represents the **Amplitude** of the graph, this is half the difference between the maximum and minimum values.

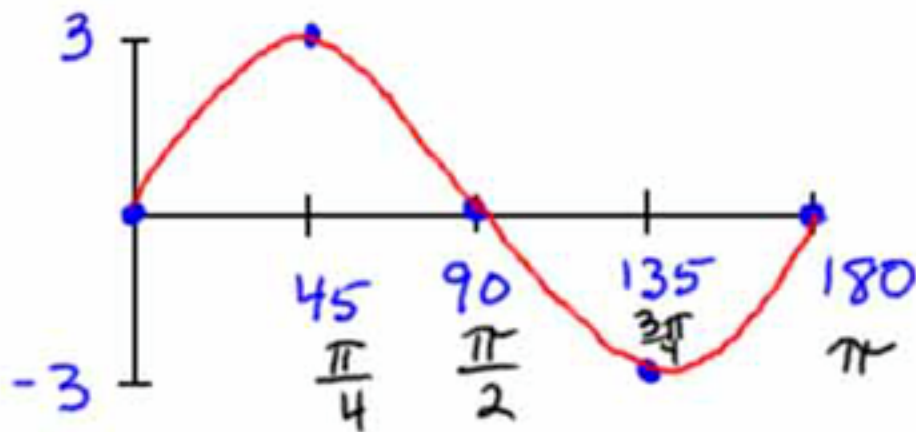
If **A** is a negative number, your graph is reflected across the  $x$ -axis.

**B** helps you find the period of the graph. To calculate the period, divide  $360^\circ$  or  $2\pi$  by the absolute value of **B**,  $|B|$ .

Let's look at some characteristics of the Sine graph:

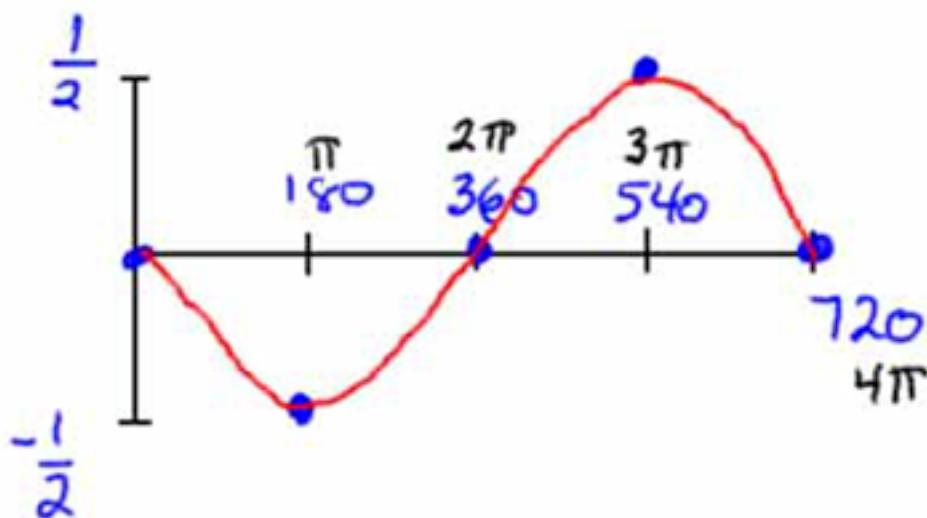
- 1) at  $0^\circ$  or 0 radians its value is 0
- 2) at one fourth of its period it reaches its maximum value
- 3) half way through its period it is 0
- 4) three fourths of its period it reaches its minimum value
- 5) at the end of its period it is again 0
- 6) if **A** is negative, the placement of the maximum and minimum values are reversed (a reflection across the  $x$ -axis).

Ex 1) Sketch the graph of:  $y = 3 \sin 2\theta$ .



Amplitude = 3  
Period =  $180^\circ$  or  $\pi$  radians

Ex 2) Sketch the graph of:  $y = -\frac{1}{2} \sin \frac{1}{2}\theta$

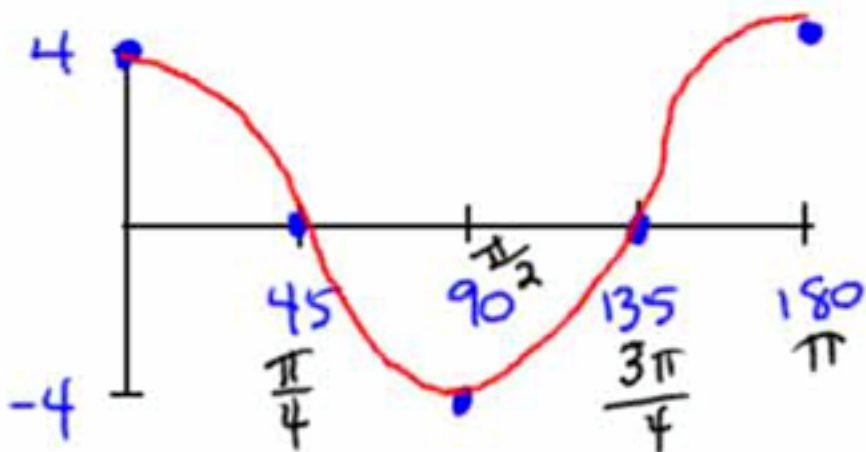


Amplitude =  $1/2$   
Period =  $720^\circ$  or  $4\pi$   
Negative sign creates reflection of graph over x-axis.

Let's look at some characteristics of the Cosine graph:

- 1) at  $0^\circ$  or 0 radians it reaches its maximum value
- 2) at one fourth of its period it is 0 (zero)
- 3) half way through its period it reaches its minimum value
- 4) three fourths of its period it is 0 (zero) again
- 5) at the end of its period it reaches its maximum value again
- 6) if  $A$  is negative, the placement of the maximum and minimum values are reversed (a reflection across the  $x$ -axis).

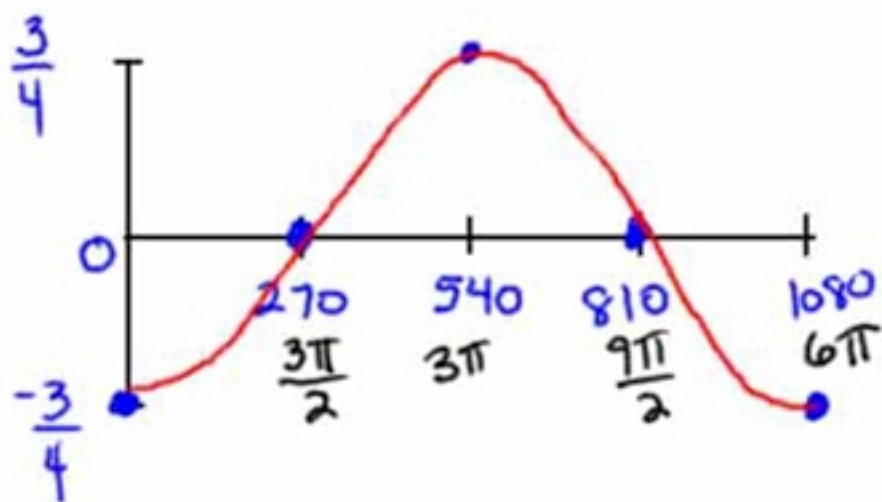
Ex 3) Sketch the graph of:  $y = 4 \cos 2\theta$



Amplitude = 4

Period =  $180^\circ$  or  $\pi$

Ex 4) Sketch the graph of:  $y = -\frac{3}{4} \cos \frac{1}{3} \theta$



Amplitude =  $\frac{3}{4}$

Period =  $1080^\circ$  or  $6\pi$